A common problem in upper division math is to prove that $\sqrt{2}$ is an irrational number. Prove that $\sqrt[3]{2}$ is an irrational number.